A new approach to scatter correction in SPECT images based on Klein_Nishina equation

Mohsen Hajizadeh Saffar¹, Shabnam Oloomi², Peter Knoll³, Hadi Taleshi⁴

¹Medical Physics Research Center, School of Medicine, Mashhad University of Medical Sciences, Mashhad, Iran
²Medical Physics Department, Mashhad University of Medical Science, Mashhad, Iran
³Department of Nuclear Medicine, Wilhelminenspital, Vienna, Austria
⁴Department of Medical Physics, Faculty of Medical Sciences, Tarbiat Modares University, Tehran, Iran

(Received 19 November 2012, Revised 1 April 2013, Accepted 7 April 2013)

ABSTRACT

Introduction: Scattered photon is one of the main defects that degrade the quality and quantitative accuracy of nuclear medicine images. Accurate estimation of scatter in projection data of SPECT is computationally extremely demanding for activity distribution in uniform and non-uniform dense media.

Methods: The objective of this paper is to develop and validate a scatter correction technique that use an accurate analytical model based on Klein_Nishina scatter equation and compare Klein_Nishina scatter estimation with triple energy window. In order to verify the proposed scattering model several cylindrical phantoms were simulated. The linear source in the cylindrical Phantoms was a hot rod filled with ⁹⁹mTc. K factor defines as the ratio of scatter resulting from MC simulation to scatter estimated from Klein_Nishina formula. Also a SPECT/CT scan of the image quality phantom was acquired. Row data were transferred to a PC computer for scatter estimation & processing of the images using MLEM iterative algorithm in MATLAB software.

Results: The scatter and attenuation compensated images by the proposed model had better contrast than uncorrected and only attenuation corrected images. The K-factors that used in proposed model doesn’t vary with different activities & diameters of linear source and they're just a function of depth and composition of pixels.

Conclusion: Based on Mont Carlo simulation data, the K_N formula that used in this study demonstrates better estimation of scattered photons than TEW. Proposed scattered correction algorithm will improve 52.3% in the contrast of the attenuated corrected images of image quality phantom.

Key words: Scatter correction; Klein_Nishina; Nuclear medicine images; Monte Carlo simulation

Published: June, 2013
http://irjnm.tums.ac.ir

Corresponding author: Shabnam Oloomi, Medical Physics Department, Mashhad University of Medical Science, Mashhad, Iran.
E-mail: shabnamolumi@gmail.com
INTRODUCTION

The presence of scattered photons in single photon emission computed tomography (SPECT) projection data causes reduction of the contrast and a loss of quantitative accuracy in reconstructed images [1-3]. Numbers of methods have been proposed to compensate the effects of scatter [4-11], many of them estimate and subtract the scattered component of the data such as dual and triple energy window. Such removal of scattered photons leads to increase statistical noise in the image, causing degradation and may outweigh the benefits of performing the scatter correction [12-14]. Alternative scatter correction methods are to correct the scattered photon based on modeling the scatter distribution. In these methods compensation is achieved, in effect, by mapping scattered photons back to their point of origin. Since all of acquired counts are used, the noise increase found with scatter subtraction methods is avoided. The accuracy of these methods depends upon the accuracy of the scatter model used, and such developed models can provide accurate three-dimensional (3-D) scatter compensation in SPECT [15-18].

In this work we introduce MLEM analytical scatter compensation model based on Klein_Nishina scatter equation [19], to achieve in SPECT images. The K and K’ factor are defined for converting the K-N and TEW scatter estimation to MC simulated phantom projection data.

The estimation of scattered photons with the Klein_Nishina formula is compared with TEW as a routine subtraction technique for scatter correction. Finally the contrast improvement, from an image quality phantom resulting from proposed algorithm compares with attenuated corrected image is shown.

METHODS

Monte Carlo Simulation

In order to verify the proposed scattering model a simulated phantoms with uniform attenuation media was established in SimSET software [20]. Simulated phantom, Figure 1, was a cylinder with 50 cm inner diameter and 30 cm height, containing a $^{99m}$Tc line source, 30 cm long at 20 cm from the center. The projection data was acquired when the cylinder axis was parallel to the bed and the phantom was filled with water. Each phantom was simulated 6 times with different line source diameters, 0.2, 1 and 4.8 cm and different activities, 10 and 40mCi, as the low and high activity used in clinic. These simulated phantoms provided an extended scattering medium and remained simple enough to expedite the analysis process.

Fig 1. a) Simulated phantom & projection, b) transverse view of phantom.

Four orders of Compton scattering was simulated and large number of photon histories were traced to create essentially low noise data. The projection data were acquired with gamma camera specifications (image size: 64×64, projection No.: 64 over 360°).

The effects of attenuation and scatter were included and data were binned into three energy windows: window1 as photo peak at 126-154 keV, Window 2 at 154-156 keV and Window3 at 92-125 keV. The primary and scatter components of the projection data were stored separately to enable verification of the scatter compensation methods described.

Phantom study

A SPET/CT scanner, GE Infinia Hawkeye, was used to acquire projection data of an image quality phantom [21], containing 4 hot spheres, 2 holes as cold spheres and an absorber in the center [22]. The background and 4 hot spheres of the phantom were filled with Tc-99m, with an activity concentration ratio of 1:8, the cold spheres activity are zero (Figure 2). Projection data were measured with 64×64 pixels, from 0-360° with 6 degree increments and stored with CT images of the phantom in DICOM format.

Fig 2. Image quality phantom.

Proposed algorithm for scatter correction

As scattered photons can be measured precisely by Monte Carlo, the estimated scatter from Klein_Nishina formula and that measured from
Scatter correction of SPECT images with Klein-Nishina equation
Hajizadeh Saffar et al.

standard Triple Energy Window (TEW) method was first converted to Monte Carlo via K and K' factors and then compared the scatter estimation based on Klein-Nishina(K_N) equation with TEW method. K and K' factors are defined as:

$$K = \frac{\text{scattering measured from Monte Carlo}}{\text{scatter estimated by K_N formula}}$$

$$K' = \frac{\text{scattering measured from Monte Carlo}}{\text{scatter estimated by TEW}}$$

As scattering seems to be dependent on source size, depth, composition of the medium and activity of the source, K factor were measured on flowing steps:

**Step 1** to assess the effect of source size on the K factor, the K factor for different line source diameters 0.2, 1 and 4.8cm were measured within same attenuation media.

**Step 2** to study the dependency of K factor to depths, the data of different projections which resembles the line source at different depths from the surface of the cylinder (5 to 45 cm) were measured.

**Step 3** to study the dependency of K factor with object composition the simulated phantom were filled with water, lung and bone respectively and measured.

**Step 4** to assess the effect of activity concentration, different activity 10 and 40mCi were injected into the line source and measured.

Finally k and K', which are obtained through simulation study, can be used in later experimental studies. It means that "K×scatter estimated by K_N formula" or "K×scatter estimated by TEW" will generate scatter photon counts that are close to scatter photons resulting from Monte Carlo simulation.

**Scatter estimation method based on K_N equation**

Numbers of authors have published descriptions of analytical equations that allow an exact calculation of scatter photons. These are quite complex, incorporating transport of photons from source to detector with probability of Compton interaction at any point [23-25]. Some of them have used differential cross section (dσ/dΩ) of photons scattered from a single free electron as a function of scattering angle (θ) proposed by K_N formula as follow to build appropriate scatter models for scatter correction in emission tomography.

$$\frac{d\sigma}{d\Omega} = \frac{1}{2}r^2P^2(E,\theta)\left(\frac{1}{P(E,\theta)^2}+P(E,\theta)\text{-1+cos}^2\theta)\right)$$

Equation 1

Where $$P(E,\theta) = \frac{1}{1+\frac{E}{mec^2}(1-\cos\theta)}$$ and $$r_e$$ is classic electron radius, $$E_0$$ is the incident photon energy and $$P(E,\theta)$$ is the ratio of photon energy after and before collision. In this paper we would present a mathematical scatter correction approach basis on K_N scatter equation. In this algorithm according to Equation 2, scattering contributions of each voxels along the detector (SC) are calculated from emission photons of 26 neighbor voxels in 3 slices (8 in the slice that voxel j belongs to, 9 in the above and 9 in the below slices) using K_N formula. The scattering photons are then summed for all voxels along each detector in a projection to form a scattered data bin, SC to be used in image reconstruction process. These data can be used in all iterations in the MLEM image reconstruction process.

$$SC_j = \sum_{c=1}^{s+1} \sum_{f=1}^{j-1} \sum_{s=1}^{J,s} K_{j,c,s} \times (K_N)_{j,c,s} \times f_{j,c,s}$$

Equation 2

Where pixel j belongs to slice s and column c, K is the aforementioned factor that corrects the Klein-Nishina scatter estimation to Monte Carlo data, K_N is the Klein-Nishina scatter count and f is the count of pixel j.

**Scatter estimation based on TEW method**

The TEW approach relies on relatively narrow energy windowsplaced close on either side of the photo-peak [9]. The scattering photons for each pixel, C_{scat}, can be calculated from the following equation:

$$C_{scat} = \left(\frac{C_{left}}{W_s} + \frac{C_{right}}{W_s}\right) \frac{W_m}{2}$$

Equation 3

Where W_m and Ws are photo peak and narrow energy window widths, C_{left} and C_{right} are the counts on left and right windows, respectively. The selection of scatter windows close to the photo-peak aims to achieve good estimation of the scatter distribution while providing a realistic estimate of the scatter fraction. This approach involves subtraction of the scatter estimate, pixel by pixel, from the photo-peak projection data.

**Image Reconstructions**

A conventional MLEM formula was used for image reconstruction algorithm as no correction images[26].
It is used with $a_{ij}(\mu) = a_{ij} \cdot e^{-\sum_{k} r_{ik} \mu_k}$ to reconstruct attenuation corrected images, which $r_{ik}$ and $\mu_k$ are respectively the length and attenuation coefficient of pixel $k$, which is along the direction of pixel $j$ to detection bin $i$. It should be mentioned that GE Infinia Hawkeye system used bilinear energy mapping to convert CT numbers to attenuation coefficients of $^{99m}$Tc [27-29]. Equation 4 was used for attenuation and scatter corrected images.

$$f_j^{p+1} = \sum_{i=1}^{n} a_{ij} \frac{g_i}{\sum_{i=1}^{n} a_{ij} [\sum_{j=1}^{m} f_j^p]^2 + SC_j}$$

$i = 1,2,3, ... n \text{ and } j = 1,2,3, ..., m$

Equation 4

Where $f_j^p$ represents pixel value of the image in $p^{th}$ iteration, $g_i$ the measured SPECT emission data, $a_{ij}$ the elements of the system matrix, $SC_j$ the scatter estimation, which is equal to sum of $SC_j$ along the direction of detection bin $i$ at $p^{th}$ iteration.

In equation 4, attenuation and scatter correction were performed using $\mu$-values from CT data of image quality phantom as an attenuation map and the proposed algorithm for scatter compensation.

To assess the effect of attenuation and scatter corrections, image contrast improvement was measured using the difference of mean target and mean background that divided by mean background of predefined ROIs. The target ROI and background ROI were selected as 3 pixels around a hot spot and 7 pixels of background through the profile.

RESULTS AND DISCUSSION

Depth dependence of K-factor to different object composition is shown on Figure 3.

![Fig 3. Variation of K-factor with depth in different medium, for 0.2 cm diameter line source; 10 mCi activity.](image)

This figure shows that variation of K-factors for 0.2 cm diameter line source and 10 mCi activities keeps the same trends in water, bone and lung. They are increased slowly with depth especially near the sources (up to 30 cm), and is nearly close to 1 for water, which means that the $K_N$ formula estimate the scattering photons close to true scattering by Monte Carlo. For lung and bone those values are lower and higher meaning that the scattering will be over and under estimate respectively by $K_N$.

To assess the effect of source size, different line source diameters with constant specific activity of 0.094 mCi/cm$^3$ were studied. Results in water phantom are shown in Figure 4.

![Fig 4. Variation of K-factor with depth in water phantom, for different line source diameter and constant specific activity of 0.094mCi/cm$^3$.](image)

In order to assess the significance of differences, a one-way ANOVA was performed on the K-factor by categorizing the source sizes. Note that the $p$-values for the $F$ statistic are lower than a 0.01 significance level. However, no significant differences in K-factors were found between 0.2, 1 and 4.8 cm line sources (e.g. P-value=0.095 between sources of 0.2 and 1 cm diameter). Activity dependence of K factor was studied with different amounts of activity (10 and 40 mCi as the lowest and highest activity used in clinic) injected into the line source. The results show no significant difference for K factors with different activities (Figure 5).

![Fig 5. Variation of K factor with depth, for different activity.](image)
Figures 4 and 5 show that variation of K factor with depth is independent of source size and activity. So in equation 2, K for each pixel is a function of depth and composition of that pixel. The rapid variation of K factor after 30 cm depth in Figures 4, 5 and 6 caused by low counts of related projections and therefore small signal to noise ratio.

To compare the capability of K_N to estimate the scatter photons with respect to TEW, variation of K/K' factors with depth for different medium were calculate and shown in Figure 6. The results showed that except for bone phantom that k and k' are nearly the same, in other media K’ is higher than K which means TEW estimate the scattering photons less than proposed K_N algorithm.

In the authors point of view it can cause by difference in the scatter estimation based on TEW and K_N. In TEW method, only the below subwindow counts were used to estimate scatter counts in the photopeak window, in other words, as the energy of photon (channel) increase in the photopeak, the proportion of scattered counts decrease in that channel according to the triangular approximation, but in K_N method the proportion of scatter photons in different energy channel changed according to special equation which is not a linear approximation, so the scatter estimation based on K_N was bigger than TEW scatter estimation.

The performance of attenuation and scatter correction via proposed method was also evaluated by the horizontal profile through a hot spot as shown on Figure 7a. Attenuation correction increased the values of the uncorrected profile while scatter and attenuation correction via proposed model decreased the values from attenuated corrected profile (Figure 8).

In Figure 8, Contrast value in uncorrected, attenuation, attenuation and scatter corrected images are 0.84, 1.95 and 2.97, respectively. That means only attenuation correction will improve the contrast by 132% and attenuation with scatter correction by 153%. In other word the proposed scatter correction method will improve 52.3% in the contrast of attenuated corrected images.

The scatter and attenuation compensated images had better contrast than the uncorrected images, so the lesions were better defined in the scatter and attenuation-compensated images. This is in agreement with the trials demonstrated that scatter & attenuation can increase contrast in SPECT studies [30].
CONCLUSION

Based on the Mont Carlo simulation data as a standard method for estimation of scattered photons, the K_N formula that used in this study demonstrates better estimation of scattered photons than TEW to be used in image reconstruction.

Proposed scattered correction algorithm can be used successfully in clinical images. It is quite fast and effectively corrects the scattered photons.

Proposed scattered correction algorithm will improve 52.3% in contrast of the attenuated corrected images.

Acknowledgements

We would like to thank from research vice-president of Mashhad University of Medical Sciences for the financial supports and appreciate the manager of Nuclear Medicine Department of Wilhelminenspital Vienna for their kind collaborations.

REFERENCES


